

Sum and Difference Identities**Find the exact value of each.**

1) $\cos 105^\circ$

2) $\cos \frac{5\pi}{12}$

3) $\sin 15^\circ$

4) $\sin \frac{19\pi}{12}$

5) $\cos 165^\circ$

6) $\tan \frac{7\pi}{12}$

7) $\tan 255^\circ$

8) $\sin \frac{5\pi}{12}$

9) $\sin 195^\circ$

10) $\tan \frac{\pi}{12}$

Simplify.

11)
$$\frac{\tan 6\theta + \tan -\theta}{1 - \tan 6\theta \tan -\theta}$$

12) $\cos 5\theta \cos 3\theta + \sin 5\theta \sin 3\theta$

13) $\cos -4\theta \cos -5\theta + \sin -4\theta \sin -5\theta$

14)
$$\frac{\tan -5u - \tan -u}{1 + \tan -5u \tan -u}$$

Verify each identity.

15) $\tan(45 + \theta) = \frac{1 + \tan \theta}{1 - \tan \theta}$

16) $\sin(\theta + 90^\circ) = \cos \theta$

17) $\sin(\pi + \theta) = -\sin \theta$

18) $\tan(\theta - 135^\circ) = \frac{\tan \theta + 1}{1 - \tan \theta}$

Answers to Sum and Difference Identities

1) $\frac{\sqrt{2} - \sqrt{6}}{4}$

5) $\frac{-\sqrt{6} - \sqrt{2}}{4}$

9) $\frac{\sqrt{2} - \sqrt{6}}{4}$

13) $\cos \theta$

2) $\frac{\sqrt{6} - \sqrt{2}}{4}$

6) $-2 - \sqrt{3}$

10) $2 - \sqrt{3}$

14) $\tan -4u$

3) $\frac{\sqrt{6} - \sqrt{2}}{4}$

7) $2 + \sqrt{3}$

11) $\tan 5\theta$

4) $\frac{-\sqrt{6} - \sqrt{2}}{4}$

8) $\frac{\sqrt{6} + \sqrt{2}}{4}$

12) $\cos 2\theta$

16) $\sin(\theta + 90)$

$$\begin{aligned} &= \sin \theta \cos 90 + \cos \theta \sin 90 \\ &= \sin \theta \cdot 0 + \cos \theta \cdot 1 \\ &= \cos \theta \end{aligned}$$

17) $\sin(\pi + \theta)$

$$\begin{aligned} &= \sin \pi \cos \theta + \cos \pi \sin \theta \\ &= 0 \cos \theta - \sin \theta \\ &= -\sin \theta \end{aligned}$$

18) $\tan(\theta - 135)$

$$\begin{aligned} &= \frac{\tan \theta - \tan 135}{1 + \tan \theta \tan 135} \\ &= \frac{\tan \theta - -1}{1 + \tan \theta \cdot -1} \\ &= \frac{\tan \theta + 1}{1 - \tan \theta} \end{aligned}$$

$$\begin{aligned} 15) \quad &\tan(45 + \theta) \\ &= \frac{\tan 45 + \tan \theta}{1 - \tan 45 \tan \theta} \\ &= \frac{1 + \tan \theta}{1 - \tan \theta} \\ &= \frac{1 + \tan \theta}{1 - \tan \theta} \end{aligned}$$