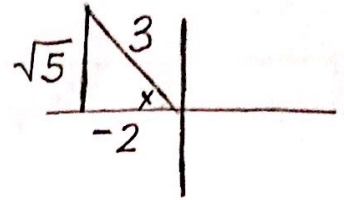


Precalculus - Unit 2 Day 3 Double Angle Identities



Evaluate each expression given $\cos x = -\frac{2}{3}$ and $\frac{\pi}{2} < x < \pi$. You can use triangles.

$$\begin{aligned}
 1. \quad \sin 2x &= 2 \sin x \cos x \\
 &= 2 \left(\frac{\sqrt{5}}{3} \right) \left(-\frac{2}{3} \right) \\
 &= \frac{-4\sqrt{5}}{9}
 \end{aligned}$$

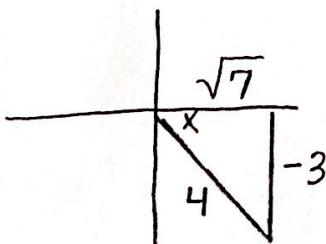
$$\begin{aligned}
 2. \quad \cos 2x &= 2 \cos^2 x - 1 = 2 \left(\cos x \right)^2 - 1 \\
 &= 2 \left(-\frac{2}{3} \right)^2 - 1 \\
 &= -\frac{1}{9}
 \end{aligned}$$

Evaluate each expression given $\sin x = -\frac{3}{4}$ and $\frac{3\pi}{2} < x < 2\pi$. You can use triangles.

$$\begin{aligned}
 3. \quad \cos 2x &= 1 - 2 \sin^2 x = 1 - 2 \left(\sin x \right)^2 \\
 &= 1 - 2 \left(-\frac{3}{4} \right)^2 \\
 &= -\frac{1}{8}
 \end{aligned}$$

$$\begin{aligned}
 4. \quad \tan 2x &= \frac{2 \tan x}{1 - \tan^2 x} = \frac{2 \tan x}{1 - (\tan x)^2} \\
 &= \frac{2 \left(-\frac{3\sqrt{7}}{7} \right)}{1 - \left(\frac{3\sqrt{7}}{7} \right)^2} \\
 &= \frac{-6\sqrt{7}}{1 - \frac{9}{7}}
 \end{aligned}$$

$$\frac{-3}{\sqrt{7}} = -\frac{3\sqrt{7}}{7}$$



$$\begin{aligned}
 &= \frac{-6\sqrt{7}}{1 - \frac{9}{7}} = \frac{-6\sqrt{7}}{\frac{7}{7} - \frac{9}{7}} = \frac{-6\sqrt{7}}{\frac{-2}{7}} = \frac{-6\sqrt{7}}{1} \cdot \frac{7}{-2} = \frac{-6\sqrt{7}}{-2} = 3\sqrt{7}
 \end{aligned}$$

Verify the identity.

5. $1 - \cos 2x \sec^2 x = \tan^2 x$

$$1 - (2\cos^2 x - 1) \sec^2 x = \tan^2 x$$

$$1 - (2\cos^2 x \sec^2 x - \sec^2 x) = \tan^2 x$$

$$1 - 2\cos^2 x \left(\frac{1}{\cos^2 x}\right) + \sec^2 x = \tan^2 x$$

$$1 - 2 + \sec^2 x = \tan^2 x$$

$$-1 + \sec^2 x = \tan^2 x$$

$$-1 + (\tan^2 x + 1) = \tan^2 x$$

6. $\sin 3x = 3\sin x - 4\sin^3 x$ $\tan^2 x = \tan^2 x$

$$\sin(\underbrace{2x}_\alpha + \underbrace{x}_\beta) = 3\sin x - 4\sin^3 x$$

$$\sin 2x \cos x + \cos 2x \sin x = 3\sin x - 4\sin^3 x$$

$$(2\sin x \cos x) \cos x + (1 - 2\sin^2 x) \sin x = 3\sin x - 4\sin^3 x$$

$$2\sin x \cos^2 x + \sin x - 2\sin^3 x = 3\sin x - 4\sin^3 x$$

$$2\sin x (1 - \sin^2 x) + \sin x - 2\sin^3 x = 3\sin x - 4\sin^3 x$$

$$\underline{2\sin x} - \underline{2\sin^3 x} + \underline{\sin x} - \underline{2\sin^3 x} = 3\sin x - 4\sin^3 x$$

Solve over the interval $[0, 2\pi)$. $3\sin x - 4\sin^3 x = 3\sin x - 4\sin^3 x$

~~X~~ $1 - \cos 2x = \sin x$

~~X~~ $2\cos x + \sin 2x = 0$