

Name: _____ Class Period: _____

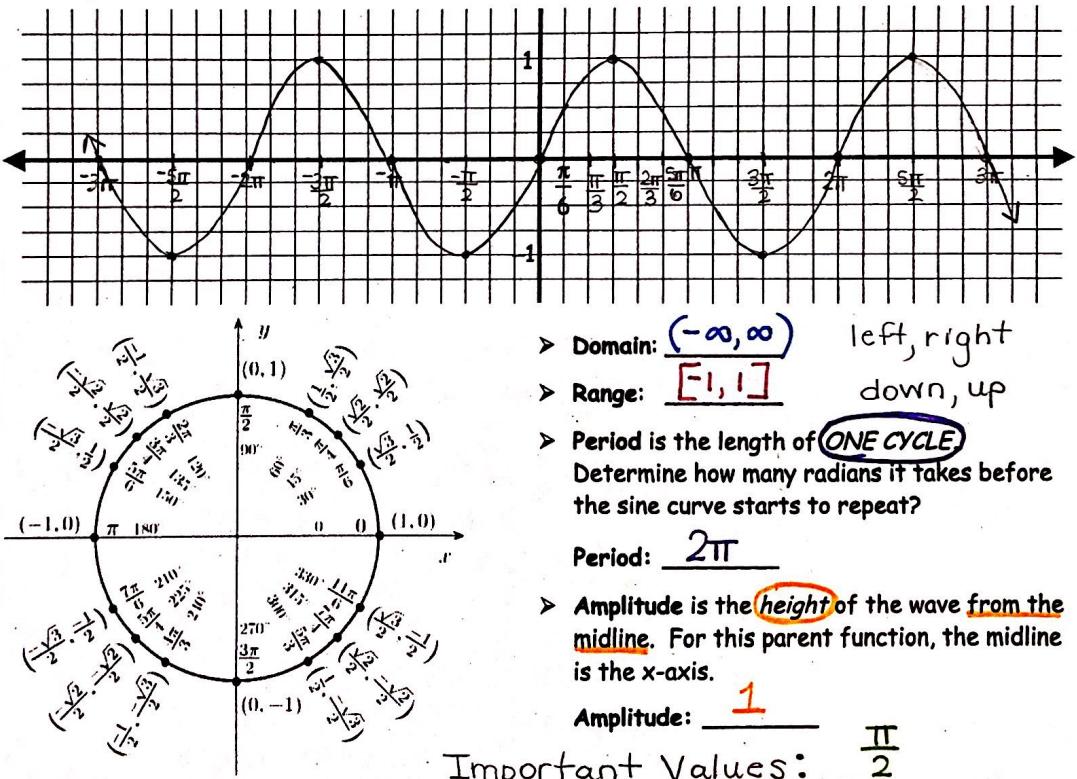
Precalculus - Unit 1 Day 6

Graphs of Sine and Cosine Functions

Graph the sine function. First complete the x-y chart by listing the corresponding radian measure for each degree measure. Strategically select angles (inputs) that have rational output values. Then, determine the y-value (output) for each x-value (input). Notice the pattern and continue graphing until the entire grid is filled. Use the unit circle to help you complete the table.

$$y = \sin(x)$$

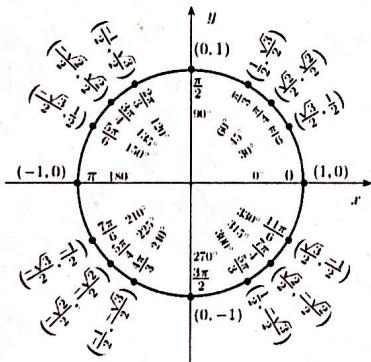
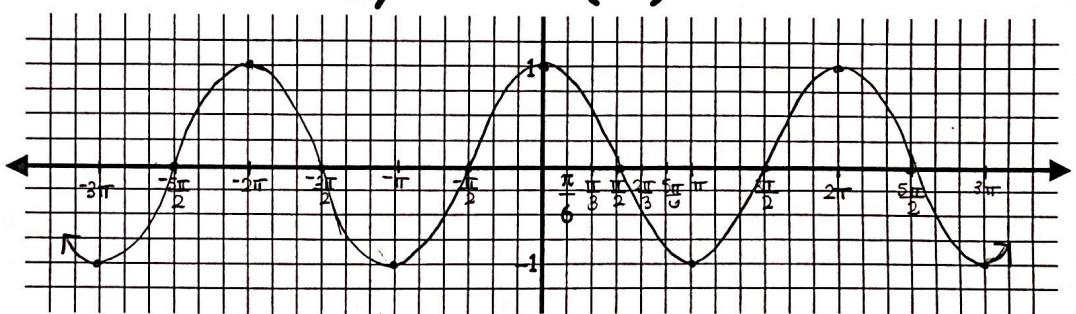
x radians	x degrees	y
-3π	-540°	0
$-\frac{5\pi}{2}$	-450°	-1
-2π	-360°	0
$-\frac{3\pi}{2}$	-270°	1
$-\pi$	-180°	0
$-\frac{\pi}{2}$	-90°	-1
0	0°	0
$\frac{\pi}{2}$	90°	1
π	180°	0
$\frac{3\pi}{2}$	270°	-1
2π	360°	0
$\frac{5\pi}{2}$	450°	1
3π	540°	0



Now, do the same thing for the Cosine Function.

$$y = \cos(x)$$

x radians	x degrees	y
-3π	-540°	-1
$-\frac{5\pi}{2}$	-450°	0
-2π	-360°	1
$-\frac{3\pi}{2}$	-270°	0
$-\pi$	-180°	-1
$-\frac{\pi}{2}$	-90°	0
0	0°	1
$\frac{\pi}{2}$	90°	0
π	180°	-1
$\frac{3\pi}{2}$	270°	0
2π	360°	1
$\frac{5\pi}{2}$	450°	0
3π	540°	-1



> Domain: $(-\infty, \infty)$

> Range: $[-1, 1]$

> Period: 2π

> Amplitude: 1

Important Values: $\frac{\pi}{2}$

Note: Functions that behave in such a repetitive (or cyclical) manner are called periodic. The graphs of the sine and cosine functions are also known as Sinusoidal (wave) graphs.

Describe the transformation(s) that occurred to the parent function, $y = \sin x$.

1. $y = 2\sin x$ vertical stretch by a factor of 2	2. $y = -\frac{1}{3}\sin x$ reflection over x-axis vertical compression by a factor of 3	3. $y = \sin(x+1)$ horizontal translation left 1
4. $y = \sin x + 2$ vertical translation up 2	5. $y = \sin(2x)$ horizontal compression by a factor of 2	6. $y = \sin \frac{x}{4}$ horizontal stretch by a factor of 4

vertical stretch/compress

$$y = -a(-bx \pm h) \pm k$$

vertical translation
up/down

reflection
over
x-axis

reflection
over
y-axis

horizontal translation
right/left

horizontal
stretch/compress

$$y = -a \sin(-bx \pm c) \pm d$$

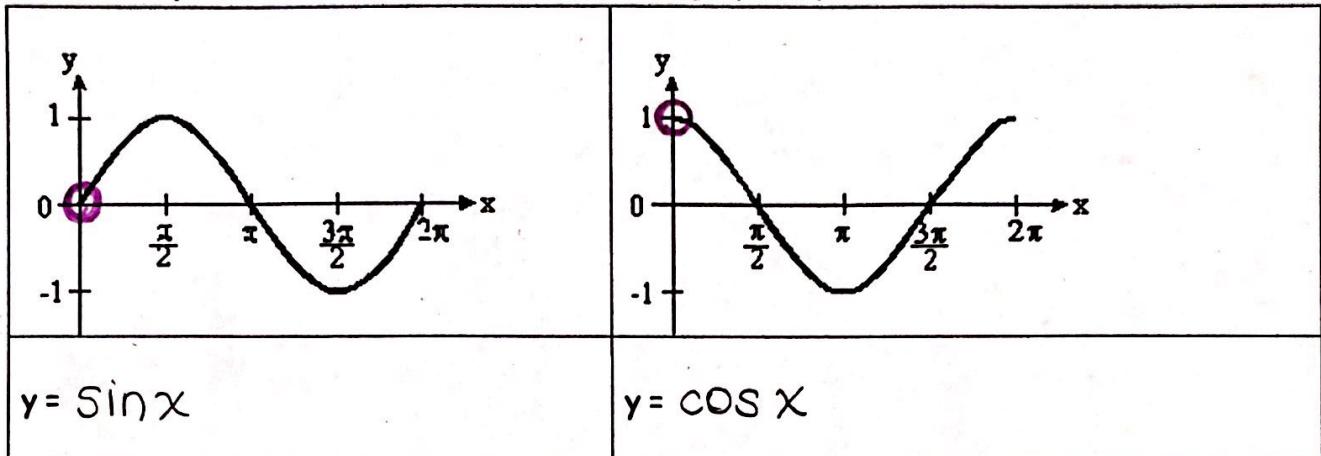
amplitude

helps us to find
the phase shift = $\frac{c}{b}$

midline

helps us find
the period = $\frac{2\pi}{b}$

Use your knowledge of transformations to graph each of the following trigonometric functions. One period of the sine and cosine function are graphed below. Identify which one is which and use the "important values" as you translate each graph in questions #1-10.

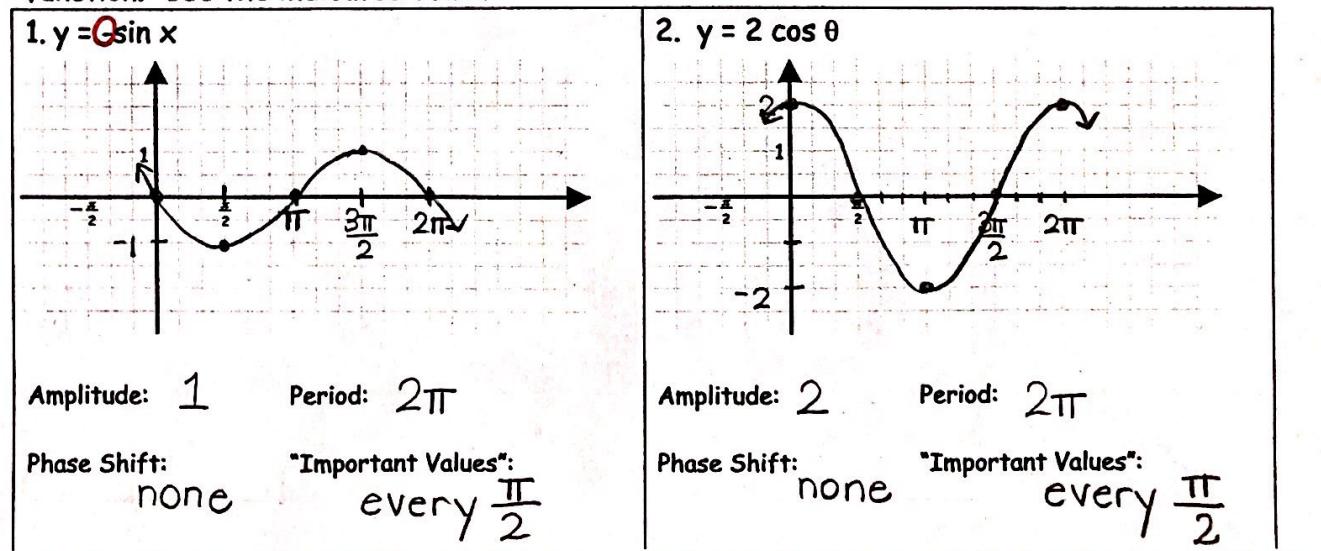


The "important values" are where the peaks, valleys and intercepts occur. The peaks and valleys are your relative extrema. For the sine and cosine function, these values happen every $\frac{\pi}{2}$ radians.

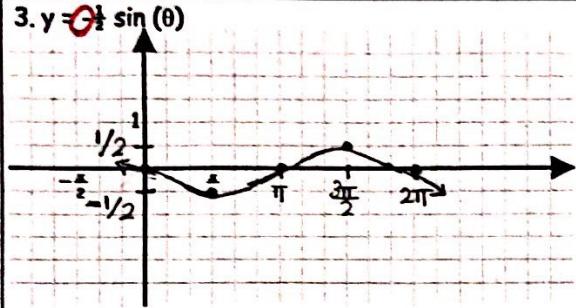
The general equations for the sinusoidal functions are:

$y = a\sin(bx - c) + d$ and $y = a\cos(bx - c) + d$			
$ a $ is the amplitude	$\frac{2\pi}{b}$ is the period	$\frac{c}{b}$ is the phase shift	d is the midline

Graph each of the following functions. Be sure to include all relative extrema and intercepts. Include at least ONE period for each function. List the amplitude and the period for each function. Use the indicated scale.



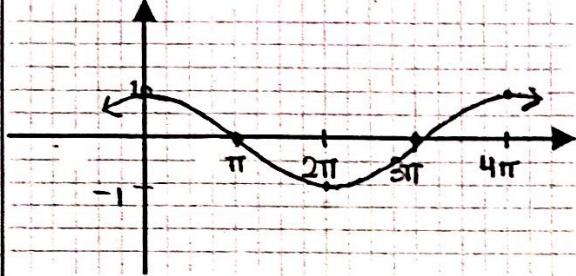
3. $y = \frac{1}{2} \sin(\theta)$



Amplitude: $\frac{1}{2}$
Phase Shift: none

Period: 2π
"Important Values": every $\frac{\pi}{2}$

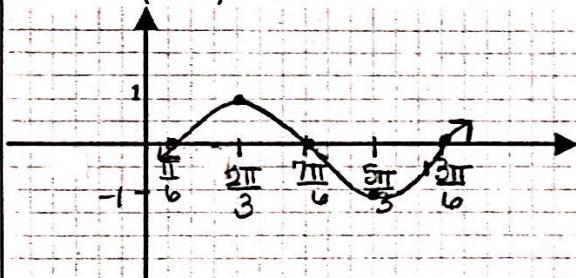
5. $y = \cos(\frac{1}{2}x)$



Amplitude: 1
Phase Shift: none

Period: $\frac{2\pi}{1/2} = 4\pi$
"Important Values": every π

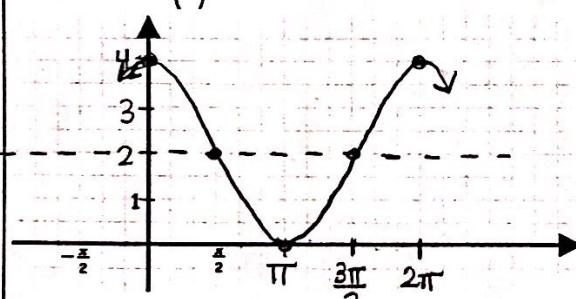
7. $y = \sin(x - \frac{\pi}{6})$



Amplitude: 1
Phase Shift: $\frac{\pi}{6} = \frac{\pi}{6}$

Period: 2π
"Important Values": every $\frac{\pi}{2}$

9. $y = 2\cos(\theta) + 2$

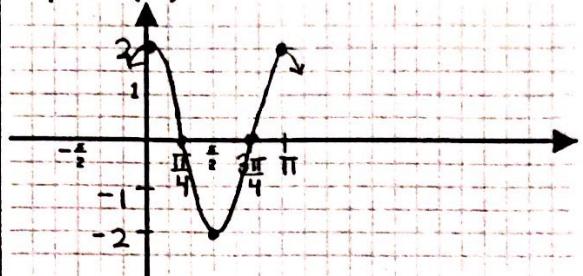


Amplitude: 2
Phase Shift: none

Period: 2π
Vertical Shift: up 2

Imp Val: every $\frac{\pi}{2}$

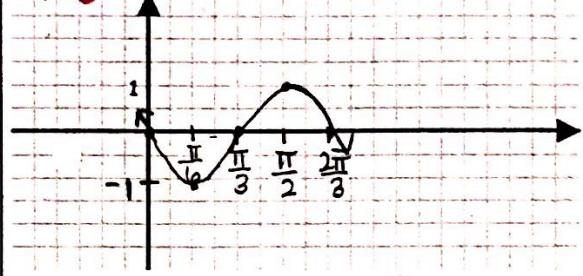
4. $y = \cos(2x)$



Amplitude: 1
Phase Shift: none

Period: $\frac{2\pi}{2} = \pi$
"Important Values": every $\frac{\pi}{4}$

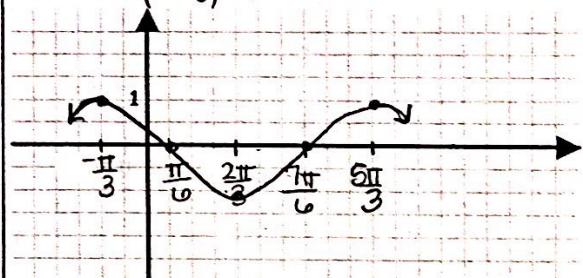
6. $y = -\sin(3\theta)$



Amplitude: 1
Phase Shift: none

Period: $\frac{2\pi}{3}$
"Important Values": every $\frac{\pi}{6}$

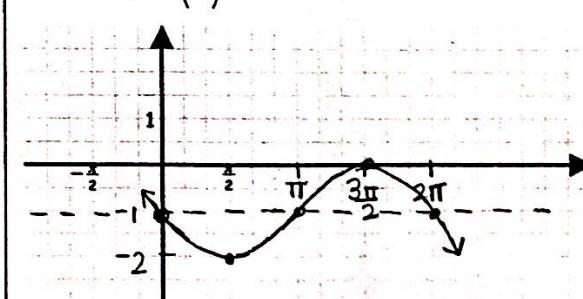
8. $y = \cos(\theta + \frac{\pi}{3})$



Amplitude: 1
Phase Shift: $\frac{\pi}{3} = \frac{\pi}{3}$

Period: 2π
"Important Values": every $\frac{\pi}{2}$

10. $y = -\sin(x) - 1$



Amplitude: 1
Phase Shift: none

Period: 2π
Vertical Shift: down 1

Imp Val: every $\frac{\pi}{2}$

Identify the amplitude and period for each of the following functions.

1. $y = 2\sin\left(\frac{1}{2}x\right) + 4$

$$\text{Period} = \frac{2\pi}{\frac{1}{2}} = 2\pi(2)$$

Amp: 2 Per: 4π

2. $y = -8\sin(6x)$

$$\text{Period} = \frac{2\pi}{6} = \frac{\pi}{3}$$

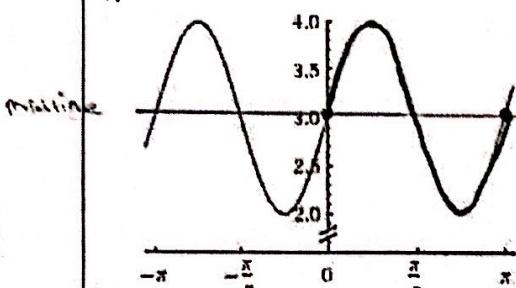
Amp: 8 Per: $\frac{\pi}{3}$

3. $y = \sin\left(\frac{2x}{5}\right)$

$$\text{Period} = \frac{2\pi}{\frac{2}{5}} = 2\pi \cdot \frac{5}{2}$$

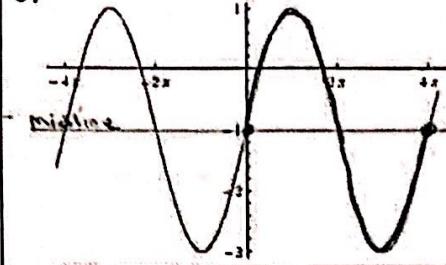
Amp: 1 Per: 5π

4.



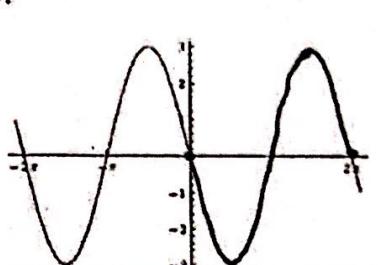
Amp: 1 Per: π

5.



Amp: 2 Per: 4π

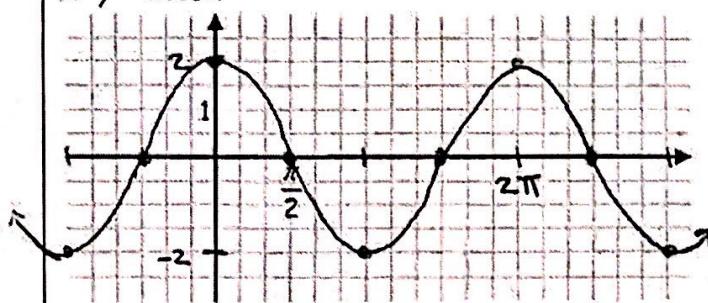
6.



Amp: 3 Per: 2π

Graph each of the functions. Be sure to include all relative extrema and intercepts. Graph as many periods of the function that will fit on the grid provided. List the requested information for each function.

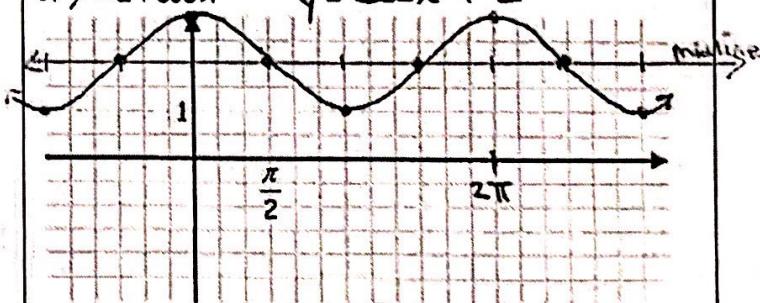
7. $y = 2\cos x$



Imp. Values: every $\frac{\pi}{2}$

Amp: 2 Per: 2π PS: 0 VS: 0

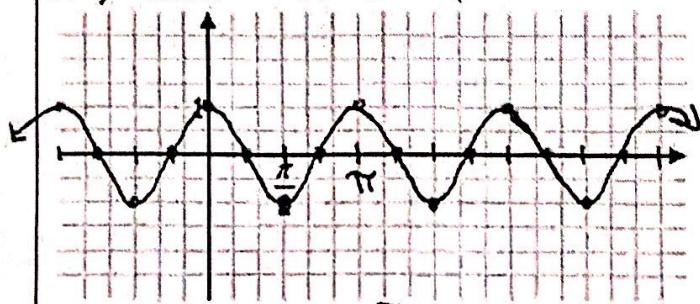
8. $y = 2 + \cos x$ $y = \cos x + 2$



Imp. Values: every $\frac{\pi}{2}$

Amp: 1 Per: 2π PS: 0 VS: 2

9. $y = \cos 2x$ Horiz. compression

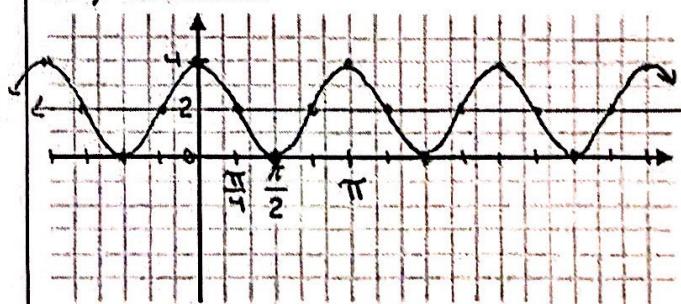


Imp. Values: every $\frac{\pi}{4}$

Amp: 1 Per: π PS: 0 VS: 0

$$\frac{2\pi}{2} = \pi$$

10. $y = 2 + 2\cos 2x$



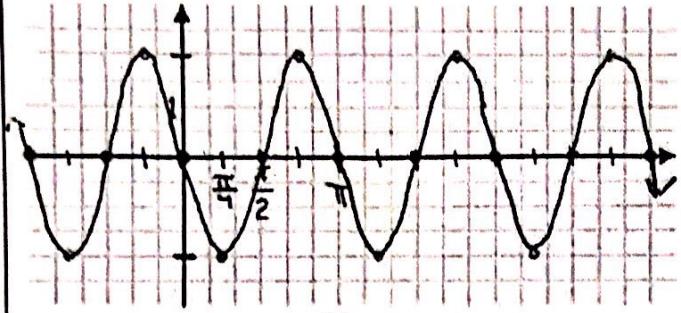
Imp. Values: every $\frac{\pi}{4}$

Amp: 2 Per: π PS: 0 VS: 2

$$\frac{2\pi}{2} = \pi$$

11. $y = -2\sin(2x)$

* reflected

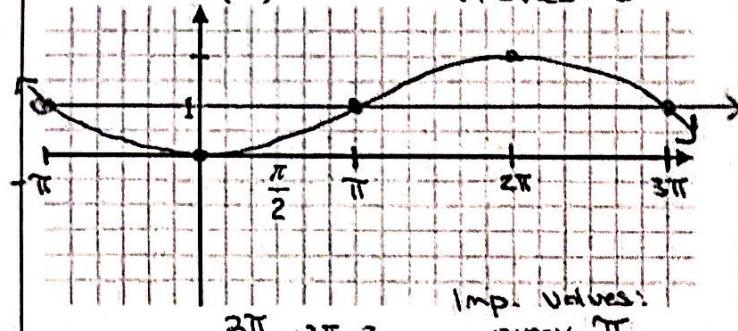


Imp. Values: every $\frac{\pi}{4}$

Amp: 2 Per: π PS: 0 VS: 0

13. $y = 1 - \cos\left(\frac{x}{2}\right)$

$y = -\cos\left(\frac{x}{2}\right) + 1$

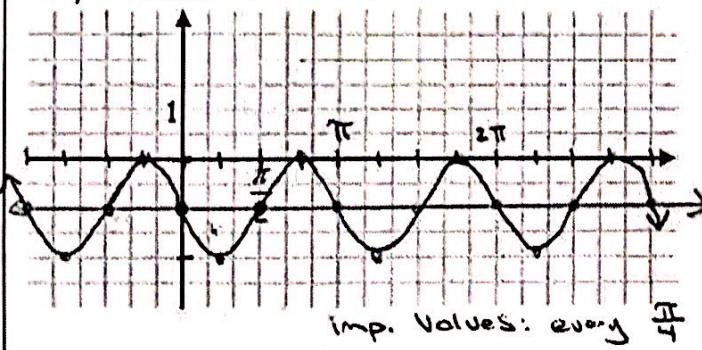


$\frac{2\pi}{\frac{1}{2}} = 2\pi \cdot 2$

Amp: 1 Per: 4π PS: 0 VS: 1

15. $y = -\sin 2x - 1$

* reflected

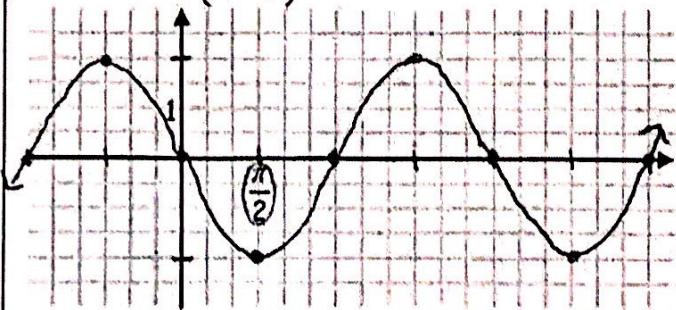


$\frac{2\pi}{2}$

Amp: 1 Per: π PS: 0 VS: -1

17. $y = -2\cos\left(x - \frac{\pi}{2}\right)$

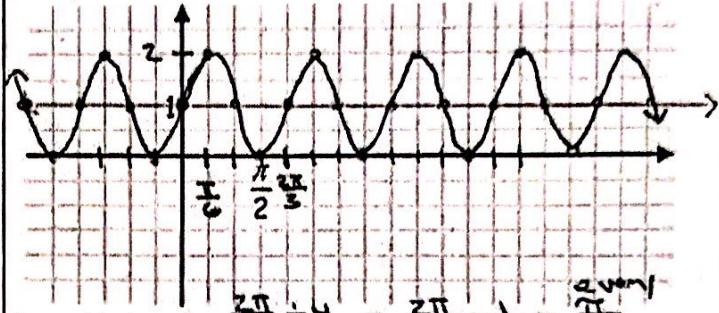
* reflected



Imp. Values: every $\frac{\pi}{2}$

Amp: 2 Per: 2π PS: $\frac{\pi}{2}$ VS: 0

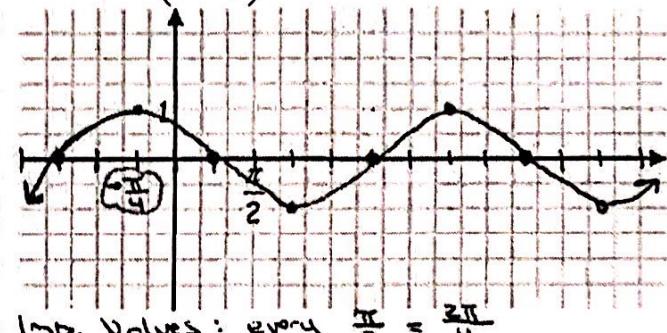
12. $y = \sin(3x) + 1$



Imp. Values: $\frac{2\pi}{3} \div 4 = \frac{2\pi}{3} \cdot \frac{1}{4} = \frac{\pi}{6}$ every

Amp: 1 Per: $\frac{2\pi}{3}$ PS: 0 VS: 1

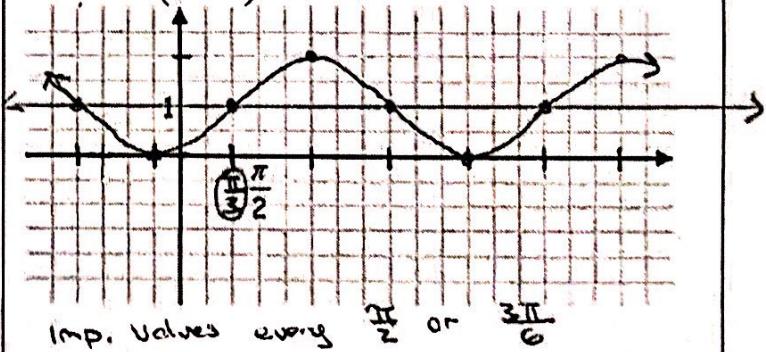
14. $y = \cos\left(x + \frac{\pi}{4}\right)$



Imp. Values: every $\frac{\pi}{2} = \frac{2\pi}{4}$

Amp: 1 Per: 2π PS: $-\frac{\pi}{4}$ VS: 0

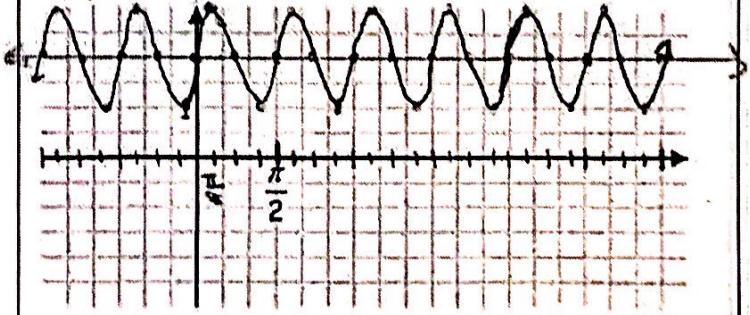
16. $y = \sin\left(x - \frac{\pi}{3}\right) + 1$



Imp. Values: every $\frac{\pi}{2}$ or $\frac{3\pi}{6}$

Amp: 1 Per: 2π PS: $\frac{\pi}{3}$ VS: 1

18. $y = 2 + \sin 4x$



Imp. Values: every $\frac{\pi}{8}$

Amp: 1 Per: $\frac{\pi}{2}$ PS: 0 VS: 2